

**EVALUATION AND ENHANCEMENT OF SOLAR PV  
HOSTING CAPACITY FOR MANAGEMENT OF  
VOLTAGE RISE IN LV NETWORKS**

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## Abstract

Proliferation of solar photovoltaics (PV) in low-voltage (LV) distribution networks is inciting technical challenges in network design and operation with regard to the quality of power. Violations of operational performance limits are increasingly evident at higher solar PV penetration levels, in particular, local voltage rise has become the major issue of concern in LV distribution networks. As the solar PV industry continues to grow, emerging challenges need to be addressed by adopting best policies and practices at a utility level. Thus, to comply with stipulated network operational limits, distribution network operators (DNOs) are compelled to develop comprehensive techniques to determine acceptable levels of solar PV hosting capacity (HC) and explore HC enhancement options.

Complexity of modelling distribution networks is a barrier for DNOs to decide levels of maximum solar PV penetration using stochastic approaches. Thus, there is a necessity to develop a systematic approach to assess solar PV HC, considering factors such as geographic layout of networks and their electrical characteristics.

This thesis extends the knowledge of managing of solar PV integration in LV networks by developing systematic approaches to evaluate solar PV HC subjected to over voltage curtailment. In this regard, a novel feeder based solar PV HC evaluation approach was developed to address the diverse network characteristics of multi feeder systems in LV distribution networks. To assess the voltage violations and critical factors affecting the solar PV HC, a comprehensive analysis of potential power quality issues was conducted on a practical LV distribution network in Sri Lanka.

The approach proposed in this thesis establishes a safe limit for solar PV HC for a given distribution feeder based on the locational and operational aspects of the solar PV units deployed on a LV network. The safe limit for HC was developed employing a number of sensitivity analyses considering factors influencing solar PV HC. Further, the proposed feeder based solar PV HC approach was extended to develop a generic method to quantify solar PV HC under different operating con-

ditions of PV inverters. Thus, it can be used as an approximate guide or a rule of thumb to evaluate solar PV HC at a given point on an LV feeder without using complex stochastic techniques.

With the increasing demand for solar PV systems, development of both solar PV HC assessment and enhancement techniques is essential in managing network voltage. DNOs have recognised the need for smart PV inverter technologies to maintain acceptable voltage levels in distribution networks. Smart PV inverters possess fast and flexible active and reactive power control functions such as; Volt-VAR and Volt-Watt control modes which can be used to manage over-voltage conditions that often limit the solar PV HC. At present, most of solar PV connection standards provide a set of rules and guidelines to mitigate voltage violations by enabling Volt-VAR and Volt-Watt control modes of the inverters. In particular, it is imperative to analyse the impact of such solar PV connection standards on HC assessment and its potential to enhance solar PV HC. Thus, a detailed analysis of smart solar PV inverter capabilities and a comparative evaluation of solar PV HC enhancement facilitated by different connection standards are presented in this thesis.

Electricity utilities around the world seek to develop strategies to increase solar PV integration while maintaining acceptable network performance. Hence, more generalised and straightforward tools are required to rapidly assess solar PV HC without complex and extensive network modelling and simulations. Extending the deterministic outcomes, a nomogram based solar PV HC assessment approach is proposed in this thesis to determine HC values specific to any location of a given conductor. Further, solar PV connection criteria is proposed which permits the electric utilities to approve new solar PV connections which facilitates reasonable modelling insights to assess HC. The proposed nomogram based solar PV HC assessment approach and solar PV connection criteria cover technical and regulatory aspects to manage PV integration in LV distribution networks.

For the continued development of solar PV as a distributed generation, accuracy of PV connection approval process is crucial to correctly and easily allow PV

connections that will not cause issues. Therefore, grid codes, distribution codes or guidelines on interconnection of solar PV require to be refined or re-written in relation to solar PV HC assessment/enhancement and approval criteria for new PV connections in LV distribution networks. The solar PV HC assessment/enhancement and solar PV connection criteria proposed in this thesis shall be a contribution to further improvement of the available guidelines/standards on solar PV installation in LV networks.

All network modeling and simulations presented in this thesis were carried out in DIGSILENT PowerFactory platform.

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## List of Principal Symbols and Abbreviations

PV	photovoltaic
HC	hosting capacity
LV	low voltage
MV	medium voltage
HV	high voltage
POC	point of connection
MCS	monte-carlo simulation
DNO	distribution network operator
GW	gigawatt
kW	kilowatt
MW	megawatt
kVAr	kilovar
kWh	kilo watt hour
ABC	aerial bundle cable
AAC	all aluminum conductor
SAM	system advisor model
AC	alternating current
DC	direct current
am	ante meridiem
pm	post meridiem
UVF	voltage unbalance factor (%)
$V_n$	neutral voltage
DNSP	distribution network service provider
$HC_{min}$	minimum hosting capacity
$HC_{max}$	maximum hosting capacity



DG	distributed generation
p.u.	per unit
$R$	resistance
$X$	inductance
$Z$	impedance
$P_{LOAD}$	active power of the load
$S_{LOAD}$	apparent power of the load in p.u.
$S_{inv}$	rating of the PV inverter
$Q_{Volt/VAr}$	required reactive power of VAr priority Volt-VAr control
$Q_{avail}$	available reactive power of Watt priority Volt-VAr control
OLTC	on-load tap changer
BESS	battery energy storage system
$P_{DG}$	total solar PV capacity
$P_{tr}$	MV/LV transformer rating
$P_{thermal\_line}$	thermal limit of the feeders,
$HC_{Feeder,Min}$	minimum hosting capacity of a given feeder
$HC_{Feeder,Max}$	maximum hosting capacity of a given feeder
$HC_{min\_LV}$	minimum hosting capacity of a given distribution network
$HC_{max\_LV}$	maximum hosting capacity of a given distribution network
$HC_{Fn\_End}$	maximum connectable solar PV capacity at the feeder end of $n^{th}$ feeder
$HC_{Fn\_Front}$	maximum connectable solar PV capacity at the feeder front of $n^{th}$ feeder
$HC^*$	solar PV hosting capacity obtained from the nomogram
$P_{PV}$	active power of PV system
$Q_{PV}$	reactive power of PV system
$P_L$	active power of the load
$Q_L$	reactive power of the load
$P$	active power
$Q$	reactive power
$V_{PV}$	voltage at the point of connection
$V_S$	voltage at the supply end
$I_S$	net current

$I_L$	load current
$I_{PV}$	net PV current
$I_{p1}$	active current component of net current when solar PV system operating at unity power factor
$I_{q1}$	reactive current component of net current when solar PV system operating at unity power factor
$I_{p2}$	active current component of net current when solar PV system operating at lagging power factor
$I_{q2}$	reactive current component of net current when solar PV system operating at lagging power factor
$I_{p3}$	active current component of net current when solar PV system operating at leading power factor
$I_{q3}$	reactive current component of net current when solar PV system operating at leading power factor
$I_{pl}$	active current component of load current
$I_{ql}$	reactive current component of load current
$V_{PV1}$	voltage at the point of connection when solar PV system operating at unity power factor
$V_{PV2}$	voltage at the point of connection when solar PV system operating at lagging power factor
$V_{PV3}$	voltage at the point of connection when solar PV system operating at leading power factor
$I_{PVp}$	active current component of PV system
$I_{PVq}$	reactive current component of PV system
$DV_l$	total voltage drop at the feeder end
$l$	feeder length
$V_b$	nominal line-line voltage
$P_S$	real power component of the total load
$Q_S$	reactive power component of the total load
$d$	distance to the POC from the distribution transformer
$P_d$	active power flow at a distance $d$ from the distribution transformer

$Q_d$	reactive power flow at a distance $d$ from the distribution transformer
$d'$	zero crossing point of active power
$Q'$	reactive power flow at a distance $d'$ from the distribution transformer
$\lambda$	ratio between the distance to POC and feeder length
$VD_l^{re}$	real component of voltage drop
$VD_l^{im}$	reactive component of voltage drop
$\Delta V$	total voltage drop made by the load across the feeder
$d''$	zero crossing point of reactive power
$pf_{pv}$	inverter operating power factor
$\theta$	voltage angle deviation
$HC_{calculated}$	HC obtained from the proposed analytical approach
$HC_{simulated}$	HC obtained from the DIgSILENT PowerFactory simulations
CIGRE	International Council on Large Electric Systems
IEC	International Electrotechnical Commission
IEEE	Institute of Electrical and Electronics Engineers
EPRI	Electric Power Research Institute
MPP	maximum power point
$V_{array}$	voltage of PV array
$I_{array}$	current of PV array
$V_{mmp-array}$	voltage in the maximum power point
$P_{conv}$	active power signal from power measurement device
E	irradiance
$V_{dc}$	DC output voltage of PV system
$I_{cap}$	differential current in DC capacitor
C	capacitance
$V_{dcin}$	output DC voltage from DC bus-bar and capacitor link
$V_{dcref}$	reference DC voltage
$V_{ac}$	measured AC voltage at the output of PV inverter
$V_{ref}$	reference AC voltage
$I_{d.ref}$	reference active power current
$I_{q.ref}$	reference reactive power current

$\cos_{ref}$	d-axis reference angle
$\sin_{ref}$	q-axis reference angle
$i_d$	d-axis current
$i_q$	q-axis current
$i_{d_{min}}$	d-axis minimum current
$i_{d_{max}}$	d-axis maximum current
$i_{q_{min}}$	q-axis minimum current
$i_{q_{max}}$	q-axis maximum current
$db$	dead-band
$ab$	active-band
$ib$	ideal-band
$K_{iq}$	reactive current droop gain
$K_{id}$	active current droop gain
$V_0$	input voltage
$P_{max}$	maximum real power output of PV inverter
$P_{min}$	minimum real power output of PV inverter
$I_{rated}$	rated current of PV inverter
VVC	volt-var control
VWC	volt-watt control
VUL	upper voltage limit
AS	Australian Standard
NZS	New Zealand Standard
HR14	Hawaii Rule 14
CR21	California Rule 21
LECO	Lanka Electricity Company
STC	standards test condition

## Publications Arising from the Thesis

### Book Chapters

1. D. Chathurangi, U. Jayatunga, S. Perera and A. Agalgaonkar, "A Generalised Deterministic Approach to Evaluate PV Hosting Capacity of LV Distribution Networks Under Different Operating Conditions," In: Zobaa A., Abdel Aleem S., Ismael S., Ribeiro P. (eds) Hosting Capacity for Smart Power Grids. Springer Cham, 2020.

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