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**NUMERICAL STUDY OF MICROCHANNEL HEAT
TRANSFER WITH NANOFLUID BASED TWO-PHASE
SLUG FLOW**

Siriwardana Sitanange Geethal Chandima Siriwardana

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degree of

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The above candidate has carried out research for the Masters thesis under my supervision.

Name of the supervisor: **Dr. P.M.T. BANDARA**

Signature of the supervisor:

UOM Verified Signature

Date: 16/05/2022

Name of the supervisor: **Dr. R.A.C.P. RANASINGHE**

Signature of the supervisor:

UOM Verified Signature

Date: 16-05-2022

ABSTRACT

Microfluidics has recently gained research attention for its high-end thermal applications, including micro heat exchangers, Lab on a Chip, micro reactors, and MEMS. It has been proven that the addition of suitable nanoparticles to a fluid can enhance the heat transfer efficiency in microchannels, both in single phase and liquid-liquid two-phase flow. In general, slug flow is said to be the most efficient in heat transfer. However, the investigation performed on liquid-liquid slug flow with added nanoparticles was found to be very limited. Hence, this study numerically investigates the heat transfer characteristics in microchannels with liquid-liquid two-phase fluid flow (water and light mineral oil) with added nano particles (Al_2O_3).

The VOF method and phase field equations were solved using ANSYS Fluent and COMSOL Multiphysics to capture two-phase flow interfaces. Adaptive mesh refinement techniques were employed to reduce computational power while maintaining sharp interfaces between fluid phases. The Eulerian mixture model was used to solve the cases containing nanoparticles. Numerical results were validated against published experimental data reported by [1] and [2].

Simulations were conducted for a 3000 micron long microchannel with a diameter of 100 microns for fluid velocity, ranging from 0.1 m/s to 0.5 m/s. First, 1 kW/cm² of heat flux is introduced to the channel wall after 1000 microns to mimic the microchip heat generation, also allowing flow to be developed.

Results have shown that using nanoparticles in either phase significantly increases heat transmission. This can be amplified even more when used in the secondary phase, by 58 percent compared with liquid-liquid two phase slug flow. This was accomplished with a nanoparticle fraction of 0.05 v/v in the secondary fluid phase. The addition of nanoparticles to the primary fluid increased heat transfer by 34%. The findings of this study can be used to improve MEMS and micro-to-macro systems that move heat.

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DEDICATION

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මෙය පිදුම් දෙමි.

I dedicate this to the

*thousands of Sri Lankans who paid and are paying taxes for the free education of
the children*

Geethal Chandima Siriwardana

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LIST OF ABBREVIATIONS

Roman Symbols

A	Correlation constant for chemical compound
B	regression coefficients for chemical Compound
Ca	Capillary Number.
Co	Confinement number
c_p	Specific heat
C_{ps}	Heat capacity of saturated liquid
D	Diameter of the microchannel
d	Nanoparticle diameter
d_a	Diameter of the aggregate
d_f	Fractal dimension of the aggregates
D_h	Hydraulic Diameter
D_i	Internal diameter
D_o	Outer diameter
e	Internal energy
e_{Di}	absolute error of the parameter D_i
F	Body force
g	Gravitational acceleration
G_z	Graetz number
k	Thermal conductivity of the fluid
K^*	Geometry dependent constants
Kn	Knudsen Number

L	Characteristics channel dimension
L_c	Microchannel length
L_{HT}	Heated length of the microchannel
L_{hyd}	Entry Length of a flow
M	Constant depends on the geometry of the channel
m	The fraction of the cross-sectional area of the tube covered with liquid.
M^*	Dimensionless quantity initiated by the author
n	Constant exponent component
Nu	Nusselt number
p	Pressure
pi	Primary fluid
Pr	Prandtl number
q	Heat flux
Q	Flow rate
r	Distance from the axis
R	Radius of the circular pipe
Re	Reynolds Number
se	Secondary fluid
T	Temperature
$T_{(r)}$	Fluid temperature at a distance of r
T_h	Dimensionless heated perimeter
T_m	Bulk mean fluid temperature
T_w	Wall temperature

u	Flow velocity
$U(r)$	Velocity component in the fully developed laminar flow
U_{avg}	Average velocity
U_B	Bubble Velocity
U_s	Slug Velocity

Greek symbols

ΔP	Pressure drop
μ	Dynamic viscosity
μ_r	Relative Viscosity
λ	Mean free path length
ρ	Local density
ρ_l	density of the liquid
ρ_v	density of the vapor
σ	surface tension
σ_i	interfacial tension between two fluids
τ	Stress tensor
Φ	nanoparticle volume fractions
σ_{l-g}	surface tension between liquid and gas
σ_{s-g}	surface tension between solid and gas
σ_{l-s}	surface tension between solid and liquid
θ_E	Young's equilibrium contact angle

Acronyms

<i>CFD</i>	Computation Fluid Dynamics
<i>CHF</i>	Critical Heat Flux
<i>CNT</i>	Carbon Nanotubes
<i>EDL</i>	Electric Double Layer
<i>EG-T</i>	Glycol/Water-Toluene
<i>EG-W</i>	Ethylene Glycol and Water
<i>EHF</i>	Extreme High Heat Flux
<i>HHF</i>	High Heat Flux
<i>LoC</i>	Lab On a Chip
<i>LVG</i>	Longitudinal Vortex Generators
<i>MCU</i>	Micro Controller Unit
<i>MEMS</i>	Micro Electromechanical Systems
<i>O/A</i>	Organic to Aqueous Volumetric
<i>PDE</i>	Partial Differential Equations
<i>SF</i>	Stagnant Film
<i>UHF</i>	Ultra High Heat Flux
<i>W-T</i>	Water-Toluene
<i>MWCNT</i>	Multi-Walled Carbon Nanotubes